



Web Ontology Language OWL Introduction to the Language

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Learning objective

• Learn Web Ontology Language OWL



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Basic Notions

Axioms: statements/propositions

- Logical assertions about the domain of discourse (real world)
 - E.g., "every eagle is a bird", "A chair has three or four legs"
- Axioms are assumed to be always true (tautologies)

Ontology

• An ontology is a set of axioms + data assertions (e.g., "Bob is an eagle")

Consistency (inconsistency)

• There is (is not) a state of affairs that satisfies statements

Main Components of an OWL Ontology

- Classes
 - Class definitions = "constructors"
- Properties
 - Object properties
 - Datatype properties
 - Annotation properties
- Individuals

Concepts (e.g. bird, eagle)

Classes are defined using properties (link individuals, e.g., married) (describe data values, e.g., name, age, date) (document ontology for human users) (e.g. Bob)



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Examples on the Next Slides are Taken from This OWL 2 Primer

OWL 2 Web Ontology Language Primer (Second Edition)

W3C Recommendation 11 December 2012

This version:

http://www.w3.org/TR/2012/REC-owl2-primer-20121211/ Latest version (series 2): http://www.w3.org/TR/owl2-primer/ Latest Recommendation: http://www.w3.org/TR/owl-primer Previous version: http://www.w3.org/TR/2012/PER-owl2-primer-20121018/ Editors: Pascal Hitzler, Wright State University Markus Krotzsch, University of Oxford Bijan_Parsia, University of Oxford Bijan_Parsia, University of Manchester Peter F. Patel-Schneider, Nuance Communications Sebastian Rudolph, FZI Research Center for Information Technology

Please refer to the errata for this document, which may include some normative corrections.

A color-coded version of this document showing changes made since the previous version is also available.

This document is also available in these non-normative formats: PDF version.

See also translations

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Abstract

The OWL 2 Web Ontology Language, informally OWL 2, is an ontology language for the Semantic Web with formally defined meaning. OWL 2 ontologies provide classes, properties, individuals, and data values and are stored as Semantic Web documents. OWL 2 ontologies can be used along with information written in RDF, and OWL 2 ontologies themselves are primarily exchanged as RDF documents. The OWL 2 Document Overview describes the overall state of OWL 2, and should be read before other OWL 2 documents.

This primer provides an approachable introduction to OWL 2, including orientation for those coming from other disciplines, a running example showing how OWL 2 can be used to represent first simple information and then more complex information, how OWL 2 manages ontologies, and finally the distinctions between the various sublanguages of OWL 2.

OWL Syntaxes

- RDF(S)-based syntaxes
- Specific OWL/XML schema
- More user-friendly notations
 - Functional-style syntax (for specifications)
 - Manchester syntax (for non-logicians)



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Classes, hierarchies, individuals (1)

- Classes and individuals
- Subclass relations
- Class equivalence and disjointness
 - Necessary and sufficient conditions
- Individual equivalence and disjointness

Functional-Style	Syntax	
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ClassAssertion(:Woman :Mary)

Functional-Style Syntax

SubClassOf(:Woman :Person)

Functional-Style Syntax EquivalentClasses(:Person :Human)

Functional-Style Syntax

DisjointClasses(:Woman :Man)

```
      Functional-Style Syntax

      SameIndividual(:James :Jim)

      Functional-Style Syntax

      DifferentIndividuals(:John :Bill)
```

Classes, hierarchies, individuals (2)

Enumerations

• Defining a class by its members

Complex classes

- Union
- Intersection

Complement

- Jack is a person but not a parent

```
Functional-Style Syntax

EquivalentClasses(

:MyBirthdayGuests

ObjectOneOf(:Bill:John:Mary)
```

Functional-Style Syntax

```
EquivalentClasses(
   :Parent
   ObjectUnionOf( :Mother :Father )
)
```

```
Functional-Style Syntax
```

```
EquivalentClasses(
:Mother
ObjectIntersectionOf(:Woman :Parent)
```

```
Functional-Style Syntax
ClassAssertion(
    ObjectIntersectionOf(
    :Person
    ObjectComplementOf( :Parent )
    )
    :Jack
)
```

Quantification

Class constructors based on quantified property values

- **Universal** restrictions All children of a happy person are happy (may have no children, too)
- Existential restrictions A parent has at least one child

Using several conditions

```
Functional-Style Syntax
 EquivalentClasses (
   :HappyPerson
   ObjectAllValuesFrom( :hasChild :HappyPerson )
Functional-Style Syntax
 EquivalentClasses(
   :Parent
   ObjectSomeValuesFrom( :hasChild :Person )
Functional-Style Syntax
 EquivalentClasses(
   :HappyPerson
   ObjectIntersectionOf(
     ObjectAllValuesFrom( :hasChild :HappyPerson )
     ObjectSomeValuesFrom( :hasChild :HappyPerson
```

Property Cardinality Restrictions

• Max cardinality John has at most 4 children Functional-Style Syntax

```
ClassAssertion(
ObjectMaxCardinality(4:hasChild:Parent)
:John
)
```

• Min cardinality John has at least 2 children

```
Functional-Style Syntax

ClassAssertion(

ObjectMinCardinality( 2 :hasChild :Parent )

:John

)
```

Exact cardinality

John has 3 children

```
Functional-Style Syntax
ClassAssertion(
    ObjectExactCardinality( 3 :hasChild :Parent )
    :John
)
```

More Property Restrictions

• Value restrictions

Functional-Style Syntax

```
EquivalentClasses(
:JohnsChildren
ObjectHasValue(:hasParent:John)
```

• Self restrictions

Functional-Style Syntax
EquivalentClasses(:NarcisticPerson ObjectHasSelf(:loves))

Property Types

Object properties

- · Relate individuals to other individuals
- :rents rdf:type owl:ObjectProperty ;

rdfs:domain :Person ;
rdfs:range :Apartment ;
rdfs:subPropertyOf :livesIn .

Datatype properties

- Relate individuals to literals of certain datatypes
- E.g., :age, :name of an individual of class Person

Annotation properties

- For labeling, commenting, etc. for human consumption
- No logical meaning for the machine!

Property Characteristics (1)

- Inverse properties
- Symmetric and asymmetric properties
- Disjointness
- Reflexive (self-relating) and irreflexive properties

Functional-Style Syntax InverseObjectProperties(:hasParent :hasChild)
Functional-Style Syntax
SymmetricObjectProperty(:hasSpouse) Functional-Style Syntax
AsymmetricObjectProperty(:hasChild)
Functional-Style Syntax
DisjointObjectProperties(:hasParent :hasSpouse

Functional-Style Syntax

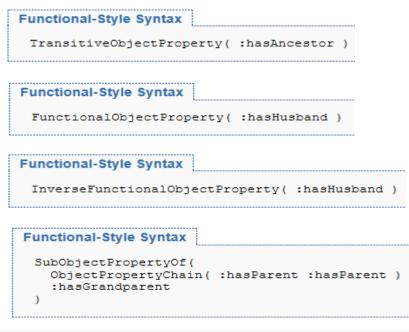
ReflexiveObjectProperty(:hasRelative)

Functional-Style Syntax

IrreflexiveObjectProperty(:parentOf

Property characteristics (2)

- Transitive properties
 - :isPartOf
- Functional properties
 - :hasNumberOfRooms
- Inverse-functional properties
 - :hasSocialSecurityID
- Subproperty relations and property chains
- Keys
 - Identify uniquely individuals by values of key properties



HasKey(:RegisteredPatient :hasWaitingListN)

```
ClassAssertion
( :RegisteredPatient :ThisPatient )
DataPropertyAssertion
( :hasWaitingListN :ThisPatient "123-45-6789"
```

Individual Facts for Populating an Ontoogy

Class and property assertions

• As in RDF

Negative assertions

• Asserting that a relation does *not* hold

Identity assertions

• owl:sameAs, owl:differentFrom, owl:allDifferent



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Setting Property Values

• Object property values

Functional-Style Syntax

ObjectPropertyAssertion(:hasWife :John :Mary)

Functional-Style Syntax

NegativeObjectPropertyAssertion(:hasWife :Bill :Mary)

- Domain/range restrictions

Functional-Style Syntax

ObjectPropertyDomain(:hasWife :Man)
ObjectPropertyRange(:hasWife :Woman)

• Datatype properties

Functional-Style Syntax

DataPropertyAssertion(:hasAge :John "51"^^xsd:integer)

Functional-Style Syntax

```
DataPropertyDomain( :hasAge :Person )
DataPropertyRange( :hasAge xsd:nonNegativeInteger )
```

Examples: OWL syntaxes

https://www.w3.org/TR/owl2-primer/

You can see and learn different syntaxes on the Primer!

Functional-Style Syntax
ClassAssertion(:Person :Mary)
RDF/XML Syntax
<person rdf:about="Mary"></person>
Turtle Syntax
:Mary rdf:type :Person .
Manchester Syntax
Individual: Mary Types: Person
OWL/XML Syntax
<classassertion> <class iri="Person"></class> <namedindividual iri="Mary"></namedindividual> </classassertion>
<classassertion> <class iri="Person"></class> <namedindividual iri="Mary"></namedindividual></classassertion>

```
Functional-Style Syntax
 EquivalentClasses(
   :Mother
  ObjectIntersectionOf( :Woman :Parent )
 )
RDF/XML Syntax
 <owl:Class rdf:about="Mother">
   <owl:equivalentClass>
    <owl:Class>
      <owl:intersectionOf rdf:parseType="Collection">
        <owl:Class rdf:about="Woman"/>
        <owl:Class rdf:about="Parent"/>
      </owl:intersectionOf>
    </owl:Class>
   </owl:equivalentClass>
 </owl:Class>
Turtle Syntax
 :Mother owl:equivalentClass [
  rdf:type owl:Class;
  owl:intersectionOf ( :Woman :Parent )
 1.
Manchester Syntax
 Class: Mother
   EquivalentTo: Woman and Parent
OWL/XML Syntax
 <EquivalentClasses>
   <Class IRI="Mother"/>
   <ObjectIntersectionOf>
    <Class IRI="Woman"/>
    <Class IRI="Parent"/>
   </ObjectIntersectionOf>
 </EquivalentClasses>
```

OWL Syntax Converter http://www.ldf.fi/service/owl-converter/



OWL Syntax Converter

OWL syntax converter is a web service for converting OWL ontologies from one syntax to another.

The service is based on OWL API.

Supported OWL syntax formats: Turtle, RDF/XML, OWL Functional Syntax, Manchester OWL Syntax, OWL/XML, Latex, and KRSS2.

Usage:

http://www.ldf.fi/service/owl-converter?onto=ONTOLOGY_CONTENT&to=FORMAT

GET/POST parameters:

- onto OWL ontology content
- to Output serialization format (ttl, rdfxml, func, manc, owlxml, latex, krss2), default: ttl

Examples:

http://www.ldf.fi/service/owl-converter?onto=<http://example.com/s>+<a>+<a>+<http://example.com /o>+.&to=func

Try the service:

OWL ontology content:

@prefix ex: <http://example.com/> .

exis a exic .



View result in browser (accept header = text/plain): Send form as HTTP POST (needed for large OWL ontology):

•

Convert

To format: Turtle

Try the service:

OWL ontology content:

```
Ontology (< http://example.com/owl/families>
   SubClassOf(
     :ChildlessPerson
     ObjectIntersectionOf (
       :Person
       ObjectComplementOf(
         ObjectSomeValuesFrom(
           ObjectInverseOf( :hasParent )
           owl:Thing
To format: Turtle
View result in browser (accept header = text/plain):
Send form as HTTP POST (needed for large OWL ontology):
```

Prefix(:=<http://example.com/owl/families/>)



@prefix : <http://example.com/owl/families#> .
@prefix owl: <http://www.w3.org/2002/07/owl#> .
@prefix rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#> .
@prefix xml: <http://www.w3.org/XML/1998/namespace> .
@prefix xsd: <http://www.w3.org/2001/XMLSchema#> .
@prefix rdfs: <http://www.w3.org/2000/01/rdf-schema#> .
@base <http://example.com/owl/families> .

<http://example.com/owl/families> rdf:type owl:Ontology .

Object Properties

http://example.com/owl/families/hasParent

<http://example.com/owl/families/hasParent> rdf:type owl:ObjectProperty .

#

#

±

Classes
#

http://example.com/owl/families/ChildlessPerson

<http://example.com/owl/families/ChildlessPerson> rdf:type owl:Class ;

Ontology Document Parts

Like RDF documents

- Namespace declarations
- Name (IRI) of the ontology
- Ontology-level metadata (versioning, comments, etc.)
- Importing other OWL documents
- Definition of classes
- Definition of properties
- Definition of individuals

See a full example in: <u>https://www.w3.org/TR/owl2-primer/</u>

Example OWL ontology from OWL 2 Primer

Prefix(:=<http://example.com/owl/families/>) Prefix(otherOnt:=<http://example.org/otherOntologies/families/>) Prefix(xsd:=<http://www.w3.org/2001/XMLSchema#>) Prefix(owl:=<http://www.w3.org/2002/07/owl#>) Ontology(<http://example.com/owl/families> Import(<http://example.org/otherOntologies/families.owl>)

Declaration(NamedIndividual(:John)) Declaration(NamedIndividual(:Mary)) Declaration(NamedIndividual(:Jim)) Declaration(NamedIndividual(:James)) Declaration(NamedIndividual(:Jack)) Declaration(NamedIndividual(:Bill)) Declaration(NamedIndividual(:Susan)) Declaration(Class(:Person)) AnnotationAssertion(rdfs:comment:Person "Represents the set of all people.") Declaration(Class(:Woman)) Declaration(Class(:Parent)) Declaration(Class(:Father)) Declaration(Class(:Mother)) Declaration(Class(:SocialRole)) Declaration(Class(:Man)) Declaration(Class(:Teenager)) Declaration(Class(:ChildlessPerson)) Declaration(Class(:Human)) Declaration(Class(:Female)) Declaration(Class(:HappyPerson)) Declaration(Class(:JohnsChildren)) Declaration(Class(:NarcisticPerson)) Declaration(Class(:MyBirthdayGuests)) Declaration(Class(:Dead)) Declaration(Class(:Orphan)) Declaration(Class(:Adult)) Declaration(Class(:YoungChild))

Declaration(ObjectProperty(:hasWife)) Declaration(ObjectProperty(:hasChild)) Declaration(ObjectProperty(:hasDaughter)) Declaration(ObjectProperty(:loves)) Declaration(ObjectProperty(:hasSpouse)) Declaration(ObjectProperty(:hasGrandparent)) Declaration(ObjectProperty(:hasParent)) Declaration(ObjectProperty(:hasBrother)) Declaration(ObjectProperty(:hasUncle)) Declaration(ObjectProperty(:hasSon)) Declaration(ObjectProperty(:hasAncestor)) Declaration(ObjectProperty(:hasHusband)) Declaration(DataProperty(:hasAge)) Declaration(DataProperty(:hasSSN)) Declaration(Datatype(:personAge)) Declaration(Datatype(:majorAge)) Declaration(Datatype(:toddlerAge)) SubObjectPropertyOf(:hasWife :hasSpouse) SubObjectPropertyOf(ObjectPropertyChain(:hasParent:hasParent) :hasGrandparent SubObjectPropertyOf(ObjectPropertyChain(:hasFather:hasBrother) :hasUncle SubObjectPropertyOf(:hasFather :hasParent

EquivalentObjectProperties(:hasChild otherOnt:child) InverseObjectProperties(:hasParent :hasChild) EquivalentDataProperties(:hasAge otherOnt:age) DisjointObjectProperties(:hasSon :hasDaughter) ObjectPropertyDomain(:hasWife :Man) ObjectPropertyRange(:hasWife :Woman) DataPropertyDomain(:hasAge :Person) DataPropertyRange(:hasAge xsd:nonNegativeInteger)

SymmetricObjectProperty(:hasSpouse) AsymmetricObjectProperty(:hasChild) DisjointObjectProperties(:hasParent :hasSpouse) ReflexiveObjectProperty(:hasRelative) IrreflexiveObjectProperty(:parentOf) FunctionalObjectProperty(:hasHusband) InverseFunctionalObjectProperty(:hasHusband) TransitiveObjectProperty(:hasAncestor) FunctionalDataProperty(:hasAge)

SubClassOf(:Woman :Person) SubClassOf(:Mother :Woman) SubClassOf(:Grandfather ObjectIntersectionOf(:Man :Parent)

/ SubClassOf(:Teenager DataSomeValuesFrom(:hasAge DatatypeRestriction(xsd:integer xsd:minExclusive "12"^^xsd:integer xsd:maxInclusive "19"^^xsd:integer SubClassOf(Annotation(rdfs:comment "States that every man is a person.") :Man :Person SubClassOf(:Father ObjectIntersectionOf(:Man:Parent) SubClassOf(:ChildlessPerson ObjectIntersectionOf(:Person ObjectComplementOf(ObjectSomeValuesFrom(ObjectInverseOf(:hasParent) owl:Thing SubClassOf(ObjectIntersectionOf(ObjectOneOf(:Mary :Bill :Meg) :Female ObjectIntersectionOf(:Parent ObjectMaxCardinality(1:hasChild) ObjectAllValuesFrom(:hasChild :Female)

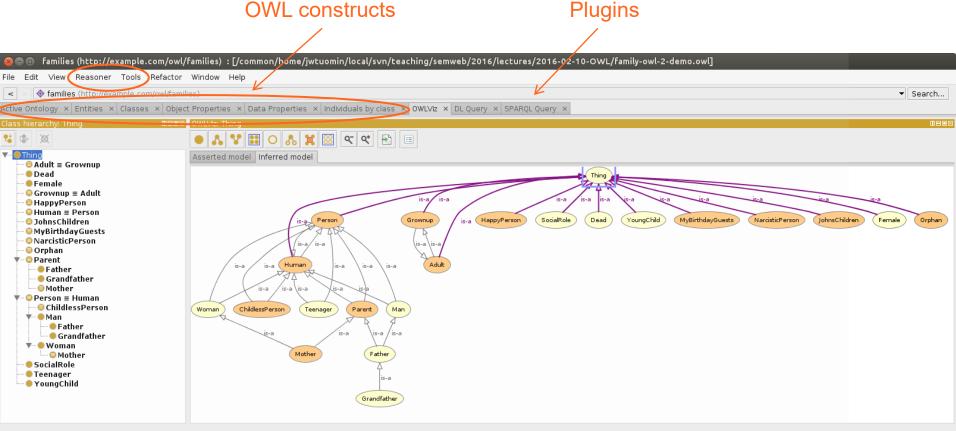
EquivalentClasses(:Person:Human) EquivalentClasses(:Mother ObjectIntersectionOf(:Woman:Parent) EquivalentClasses(:Parent ObjectUnionOf(:Mother:Father) EquivalentClasses(:ChildlessPerson ObjectIntersectionOf(:Person ObjectComplementOf(:Parent) EquivalentClasses(:Parent ObjectSomeValuesFrom(:hasChild :Person) EquivalentClasses(:HappyPerson ObjectIntersectionOf(ObjectAllValuesFrom(:hasChild :HappyPerson) ObjectSomeValuesFrom(:hasChild:HappyPerson) EquivalentClasses(:JohnsChildren ObjectHasValue(:hasParent:John) EquivalentClasses(:NarcisticPerson ObjectHasSelf(:loves)

ObjectPropertyAssertion(:hasWife :John :Mary) NegativeObjectPropertyAssertion(:hasWife:Bill:Mary) NegativeObjectPropertyAssertion(:hasDaughter :Bill :Susan DataPropertyAssertion(:hasAge :John "51"^^xsd:integer) NegativeDataPropertyAssertion(:hasAge :Jack "53"^^xsd:integer) SameIndividual(:John:Jack) SameIndividual(:John otherOnt:JohnBrown) SameIndividual(:Mary otherOnt:MaryBrown) DifferentIndividuals(:John:Bill) EquivalentClasses(:MyBirthdayGuests ObjectOneOf(:Bill:John:Marv) ClassAssertion(:Person:Mary) ClassAssertion(:Woman:Mary) ClassAssertion(ObjectIntersectionOf(

:Person ObjectComplementOf(:Parent)) :Jack) ClassAssertion(ObjectMaxCardinality(4:hasChild:Parent) :John) ClassAssertion(ObjectMinCardinality(2:hasChild:Parent) :John

```
ClassAssertion(
 ObjectExactCardinality( 3 :hasChild :Parent )
 :John
ClassAssertion(
 ObjectExactCardinality( 5 :hasChild )
 :John
ClassAssertion(:Father:John)
ClassAssertion(:SocialRole:Father)
ObjectPropertyAssertion( :hasWife :John :Mary )
NegativeObjectPropertyAssertion(:hasWife:Bill:Mary)
NegativeObjectPropertyAssertion(
 :hasDaughter
 :Bill
 :Susan
DataPropertyAssertion(:hasAge:John "51"^^xsd:integer)
NegativeDataPropertyAssertion( :hasAge :Jack "53"^^xsd:integer )
SameIndividual(:John:Jack)
SameIndividual(:John otherOnt:JohnBrown)
SameIndividual(:Mary otherOnt:MaryBrown)
DifferentIndividuals(:John:Bill)
```

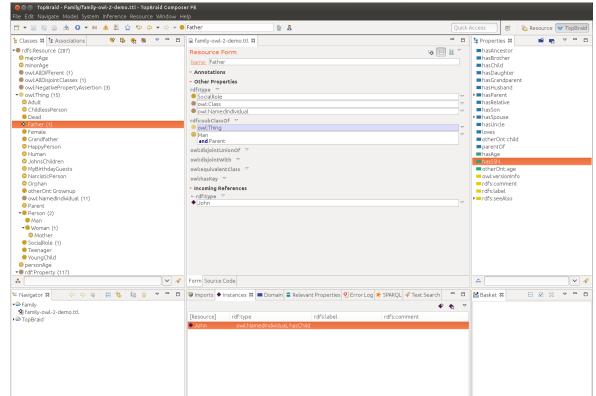
Example ontology in Protégé editor



Reasoner active 🔽 Show Inferences

...and in TopBraid Composer

- Commercial product with a free edition option
- SPIN rules for reasoning, e.g., OWL RL support available
- Includes possibility for SPARQL querying



Two Logical Assumptions of OWL



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Closed World Assumption (CWA)

Closed-world assumption: what is not known to be true is false

- Assumes that everything is known, and data not stated is assumed to be false
- Very powerful and often useful assumption
 - In use in, e.g., databases
- The notion of defaults leads to nonmonotonic logics

OWL adopts the open-world assumption:

- CWA is not made
- On the huge and only partially knowable WWW, this is a correct assumption
- Lots of additional assertions may be needed for closing data
 - For stating what facts are not true in addition to what is true

Unique Names Assumption (UNA)

- Typical database applications assume that individuals with same/different names are indeed same/different individuals
- OWL follows the usual logical paradigm where this is **not** the case
 - Plausible on the WWW where multiple IDs exist
- One may want to indicate portions of the ontology for which the assumption does or does not hold
 - In many cases UNA is useful
 - Lots of additional assertions may then be needed for stating what objects are different and what are the same

OWL Profiles: Trade-off between Expressive Power and Efficient Reasoning



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Compatibility of OWL with RDF(S): OWL Full

OWL 2 Full

- All OWL features added on top of RDF(S)
 - Allows, e.g., redefining the meaning of RDF(S) and OWL primitives
- Advantages
 - Fully upward compatible with RDF
 - Any RDF document is an OWL 2 Full document
 - Any RDF(S) conclusion is an OWL 2 Full conclusion
 - RDF-based semantics
- Disadvantages
 - Undecidable, as RDFS already has some very powerful modeling primitives
 - Complete and efficient reasoning not possible

Compatibility of OWL 2 with RDF(S): OWL DL

OWL 2 DL (Description Logic)

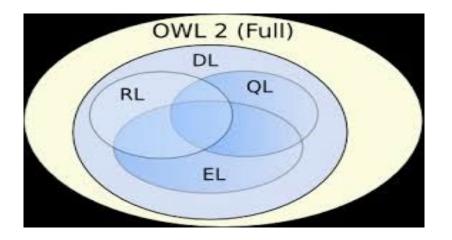
- Restricted form of OWL Full for which decidable, efficient support for reasoning is possible
 - OWL 2 primitives cannot be applied to themselves
 - Only classes of non-literal resources considered
 - Strict separation between datatype and object properties
 - Strict separation between an individual, a class, or a property
 - Using "punning" the same name may be used for different purposes, but treated as different views on the same IRI, interpreted semantically as if they were distinct
- Direct semantics, based on Description logics (Terminology logics)
 - Subsets of predicate logic
 - But also RDF-based semantics can be applied to OWL 2 DL ontologies
- Reasoning engines are available for DL
 - Pellet, FaCT, RACER, HermiT

OWL 2 profiles

OWL 2 DL includes three specific profiles for different use cases

- OWL 2 EL
- OWL 2 QL
- OWL 2 RL

Each profile includes a subset of OWL DL features



OWL 2 EL ("*EL* **description logics**")

- Good for ontologies with lots of classes and/or properties
- Polynomial complexity of standard inference types: satisfiability, classification, instance checking
- Used for large scale class ontologies, e.g., Snomed CT
- Limitations include:
 - Negation and disjunction not supported
 - Universal quantification on properties
 - E.g., "all children of a rich person are rich" cannot be stated
 - All kinds of role inverses are not available
 - *E.g.*, parentOf and childOf cannot be stated as inverses

OWL 2 QL ("query language")

- Good for querying large numbers of individuals
- Relational Query Languages (conjunctive queries)
 - Can be implemented efficiently using relational databases

- Limitations include:
 - Existential quantification of roles to a class expression
 - E.g., it can be stated that every person has a parent, but not that every person has a female parent
 - Property chain axioms and equality are not supported

OWL 2 RL ("rule language")

- Good for rule-based reasoning, database focus
- Can be implemented using logic programming
 - First-order implications: IF certain triples exist THEN add additional triples
 - See partial axiomatization of the OWL 2 RDF-based semantics as rules in the OWL 2 Profiles specification (Section 4.3)
- Limitations include:
 - Statements where the existence of an individual enforces the existence of another individual
 - E.g., the statement "every person has a parent" is not expressible
 - Restricts class axioms asymmetrically
 - Constructs for a subclass cannot necessarily be used as a superclass
- An implementation of OWL RL is used in the exercises for reasoning

Summary

- OWL 2 extends RDF(S)
- Multiple corresponding syntaxes
 - RDF notations (RDF/XML, Turtle, etc.), OWL/XML, Functional-style, Manchester syntax
- Two corresponding semantics: Direct and RDF-based
- Two OWL versions
 - OWL 2 DL: Direct semantics based on Description Logics
 - Decidable, efficient reasoning
 - Not fully upward compatible with RDF(S)
 - OWL 2 Full: Based on RDF semantics
 - Undecidable, partial reasoning possible
 - Upward compatible with RDF(S)
- Three more efficient DL profiles for different purposes
 - OWL 2 EL, OWL 2 QL, and OWL 2 RL

References and Further Information

Namespace IRI of OWL contains the specification in RDF for 1) classes and 2) properties

• <u>http://www.w3.org/2002/07/owl#</u>

Theory

- M. Krötzsch, F. Simančík, I. Horrocks: <u>Description Logic Primer</u>. 2013.
- P. Hitzler, M. Krötzsch, S. Rudolph: Foundations of Semantic Web Technologies. CRC Press, 2009.

Reasoners

• <u>http://semanticweb.org/wiki/Category_Reasoner</u>