

# Combining Ontologies and Markov Logic Networks for Statistical Relational Mobile Network Analysis

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**Abstract.** Mobile networks are managed by means of operations support systems (OSS) which facilitate performance, fault, and configuration management. Network complexity is increasing due to the heterogeneity of cell types, devices, and applications. Characterization and configuration of networks optimally in such a scenario is a challenging task. This paper introduces an experimental platform that combines statistical relational learning and semantic technologies by integrating a mobile network simulator, Markov Logic Network model (MLN) and an OWL 2 ontology into a runtime environment tool. Our experiments, based on a prototype implementation, indicate that the combination of OWL and MLN reasoning can be effectively utilized in network status characterization, optimization and visualization.

## 1 Introduction

Mobile networks have become a crucial part of our society, and yet their significance will increase in the future, as the number of users, devices, and applications are expected to drastically increase [5]. Thus, the future 5G networks need to cater for a massive increase in data volume and number of terminals, the latter due to the widespread adoption of Internet of Things (IoT) [12].

Networks need to be configured optimally to provide customers a high service quality with low operational expenses. In legacy systems, network configurations have been handled manually, but due to the increasing complexity of networks, more automation is needed from Operations and Support Systems (OSS) [10]. Currently researched and standardized technology in the telecommunication field is Self-Organizing Networks (SON), which is essentially a closed-loop agent system reacting to measurements, typically by means of a fixed rule base [10]. The challenge with this approach is creating and maintaining the rule bases in view of geographic and temporal variety on a cell level of radio access networks.

Machine Learning (ML) is expected to increase the level of automation in the OSS field by, for example, analyzing traffic patterns and cell-related data to learn statistical correlations. The output of an ML system can be characterized as hypothetical in contrast to deterministic results of a traditional rule-based system. In the long run, it has been argued that knowledge models would bring benefits as a basis of future telecommunication systems both in view of systems design and also from the perspective of value networks [18].

In this paper we propose a new approach to automated mobile network management by using statistical relational learning with a Markov Logic Network model (MLN) [20] for handling uncertainty in mobile network analysis. In addition to the MLN model, we propose an OWL 2 ontology above it to provide global meaning and description logic (DL) reasoning capabilities to the system.

The paper is divided as follows: after presenting a short view of our system, section 3 briefly presents the MLN and how it is applied to our implementation. After this section 4 describes our OWL 2 model and section 5 presents dataset statistics and how MLN reasoning results can be examined via an RDF-based GUI. Finally, section 6 discusses related work and section 7 concludes the paper and presents ideas for future work.

## 2 System Overview

The novel idea of our system is to combine uncertain and semantic modeling in an automated OSS system. The system contains a mobile network (LTE) simulator, an MLN model for statistical reasoning, an OWL 2 model for semantic modeling and a GUI for representing and interacting with the system. We simulate a small urban area with 5000 citizens (network users) and with 32 cells.

The interface between the LTE simulator and the MLN model contains OSS management activities, such as reading performance data from the simulator and sending configuration data back to it. The performance data contains key performance indicators (KPIs) for various measurement cases. KPIs utilized in the MLN model are channel quality indicator (CQI) for measuring the signal quality of a cell and radio link failures (RLF) for measuring the amount of connection failures per cell. The configuration management contains changes in the transmission power (TXP) and angle (remote electrical tilt, RET) of a cell antenna.

The MLN model processes the performance data into evidence that is used in the MLN reasoning. The reasoner infers posterior marginal probabilities for potential network configuration changes. The model parameters of the MLN reasoner can be fitted based on historical performance data and executed configuration actions. The OWL 2 model is constructed by transforming the MLN reasoner's model into a *SHIF* OWL 2 DL ontology that can be utilized with a Pellet reasoner<sup>1</sup>. In addition to DL reasoning capabilities, the OWL 2 ontology is published as an RDF graph in a SPARQL endpoint. An operator interface for managing the system and the underlying mobile network is implemented on top of the SPARQL endpoint in HTML5.

## 3 Markov Logic Network Model

This section briefly introduces the Markov logic [20] by giving a definition of the MLN, explaining the inference of marginal probabilities, and describing how the MLN is adapted to our OSS system.

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<sup>1</sup> <https://github.com/Complexible/pellet>

### 3.1 Definition

MLNs allow uncertainty and contradictory knowledge in a first-order logic (FOL) model by introducing a weight parameter for each formula in the FOL knowledge base. The weighted set of formulas defines a template for a Markov network, in which the cliques and clique potentials are determined by the formulas and formula weights.

**Definition 1.** A Markov logic network  $L$  is a set of pairs  $(F_i, w_i)$ , where  $F_i$  is a first-order formula and  $w_i$  is a real-valued weight parameter. Together with a set  $C$  of constant terms, over which the formulas in  $L$  are applied, it defines a Markov network  $M_{L,C}$  with a binary variable for each possible grounding of each predicate appearing in  $L$  and a feature for each possible grounding of each formula in  $L$ . The value of the feature corresponding to a grounding of formula  $F_i$  is 1 if the ground formula is true, and 0 otherwise. The weight of the feature is  $w_i$ , the weight associated with  $F_i$  in  $L$ .

Each state of the variables in a Markov network  $M_{L,C}$  represents a possible world, i.e., a truth assignment for each of the ground atoms for  $(L, C)$ . The probability distribution over possible worlds  $x \in \mathcal{X}$  specified by  $M_{L,C}$  is

$$P(X = x) = \frac{1}{Z} \exp \left( \sum_i w_i n_i(x) \right), \quad (1)$$

where  $n_i(x)$  is the number of true groundings of  $F_i$  in  $x$  and  $Z$  is a partition function given by  $Z = \sum_{x \in \mathcal{X}} \exp(\sum_i w_i n_i(x))$ . Intuitively this means that the weights of the true ground formulas give the logarithmized factors of the distribution function. If two worlds differ only on a single ground formula, then the weight of the formula gives the logarithmic odds of choosing one world over the other.

### 3.2 Inference

A typical inference task is to infer the most likely state or a marginal distribution of some subset of the variables using the values of all other variables as evidence. In practice, exact inference over an MLN model is infeasible. Richardson and Domingos [20] introduce an efficient stochastic algorithm for this problem.

### 3.3 Application in OSS setting

We define our MLN model in terms of three types of predicates:

- *Context predicates* indicate the current status of the network and the environment. A context predicate can indicate, for example, that some KPI value for a cell is currently below the acceptable level or that two cells are neighbors in the network topology.
- *Objective predicates* indicate required changes to KPI values to achieve performance targets defined by the operator. For example, an objective predicate can indicate that a particular KPI value for some cell is too low and needs to be increased.
- *Action predicates* indicate changes to network configuration parameter values.

Each predicate represents an attribute of a cell in the network or a relation among the cells. The domain of a predicate can be either the set of cells  $X$  or an  $n$ -ary Cartesian product of  $X$ .

The MLN model is composed of rules with these predicates. We wish the rules to describe a correlation between a set of *Objectives* and a set of *Actions* in a certain *Context*. A typical inference task is to query for appropriate actions using the current context data and objective requirements as evidence. Therefore, the rule format is defined as

$$C(x) \Rightarrow (\mathcal{O}(x) \Leftrightarrow \mathcal{A}(x)).$$

*Example 1.* Let  $L$  be a simple MLN model consisting of the weighted rules defined in Table 1. Here variables  $c$  and  $d$  denote a cell in the mobile network. Suppose that

$w_i$	$F_i$
0.5	$HighRlf(c) \Rightarrow (DecRlf(c) \Leftrightarrow IncTxp(c))$
0.2	$HighRlf(c) \Rightarrow (DecRlf(c) \Leftrightarrow DecRet(c))$
0.7	$(Neighbor(c, d) \wedge LowCqi(c)) \Rightarrow (IncCqi(c) \Leftrightarrow (DecRet(c) \wedge IncTxp(d)))$

**Table 1.** Examples of weighted rules in the MLN model

we have a mobile network with two neighbor cells named  $C1$  and  $C2$  and that we measured a low CQI value for cell  $C1$  and high RLF value for  $C2$ . We would like to use this information to infer proper configuration actions to get the CQI and RLF values to a normal level. We use the MLN reasoner to query the MLN model  $L$  for marginal probability distributions for action proposals  $IncTxp(c)$ ,  $DecTxp(c)$ ,  $IncRet(c)$ , and  $DecRet(c)$  for each cell  $c$  given the evidence:

$$E = \{Neighbor(C1, C2), LowCqi(C1), HighRlf(C2), IncCqi(C1), DecRlf(C2)\}$$

An example of the reasoning output is shown in Table 2, which shows inferred marginal probabilities for cell configurations.

$Action$	$P(Action L, E)$	$Action$	$P(Action L, E)$
$IncTxp(C1)$	0.32	$IncRet(C1)$	0.27
$DecTxp(C1)$	0.36	$DecRet(C1)$	0.50
$IncTxp(C2)$	0.56	$IncRet(C2)$	0.31
$DecTxp(C2)$	0.24	$DecRet(C2)$	0.37

**Table 2.** Marginal probabilities for cell configurations

## 4 OWL 2 Model

The OWL 2<sup>2</sup> ontology generalizes (with URIs and semantic annotation) terms and variables used in the MLN reasoning into a *SHIF* DL knowledge base. Logically, the ontology consists of two subontologies: the OSS and MLN ontology. A semantic mapping between the OSS and MLN ontologies will enhance the interoperability between the heterogeneous mobile network environment and with the MLN rule base extracted from it.

### 4.1 OSS Ontology

The OSS ontology describes network context retrieved from the LTE simulator and used by the MLN reasoner as evidence. Figure 1 briefly depicts the TBox structure of the OSS ontology. The most fundamental class in the model is *Cell* which defines 1) network topology with a *cellHasNeighbor* relation to other *Cell* instances, 2) configuration parameters with a *cellHasParameter* relation to *Parameter* instances, and 3) performance measurements with a *cellHasIndicator* relation to *Indicator* instances. The current version of the OSS ontology models the MLN evidence rather than network context generally. Thus, the only subclasses for *Parameter* are *Txp* and *Ret* and for *Indicator*, *Rlf* and *Cqi*. The *Parameter* and *Indicator* instances can be related to events by the property *cellHasEvent*, such as configurations inferred by the MLN model. Events are instances of the class *Event* where the value of the property *eventHasImpact* is an instance of *Impact* (Decrease or Increase) with a numerical value indicating the current and previous values.

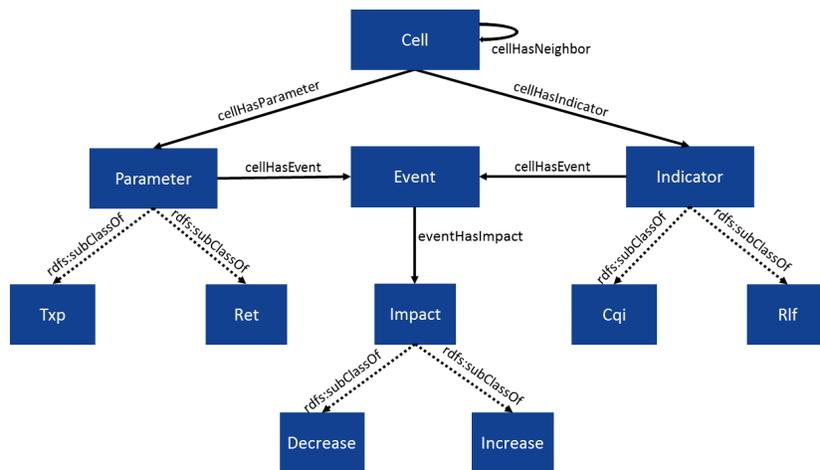
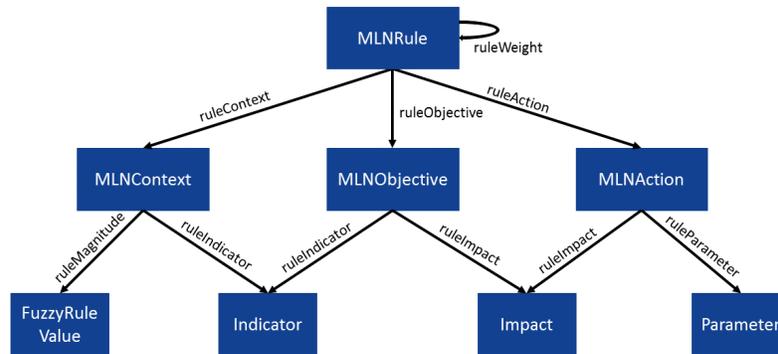


Fig. 1. The OSS ontology TBox

<sup>2</sup> <https://www.w3.org/TR/owl2-overview/>

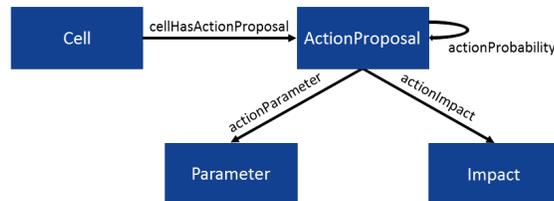
## 4.2 MLN Ontology

The MLN ontology can be seen as an OWL 2 interpretation of the MLN evidence and action proposals that are semantically bound to mobile network concepts. Figure 2 depicts a TBox model of an MLN rule. The `MLNRule` class defines a rule and it has a numerical value `ruleWeight` defining its weight and relations to rule parts `Context`, `Objective`, and `Action`. The figure also shows that the rule parts are bound to network classes `Parameter`, `Indicator`, and `Impact`. For example, an `MLNAction` class has a relation to a subclass of `Parameter` (e.g. `Txp`) and to a subclass of `Impact` (e.g. `Increase`). Similarly, `MLNObjective` have relations to subclasses of `Indicator` and `Impact` and `MLNContext` have relations to a subclass of `Indicator` and to a crisp value of an indicator (`High`, `Medium`, or `Low`).



**Fig. 2.** Rules in the MLN ontology TBox

Figure 3 shows how an `ActionProposal` class is modeled in the MLN ontology. `Cell` has a relation to `ActionProposal` whose content is defined with relations to an `Impact` and `Parameter` (for example `Increase` and `Txp`). Moreover, the numeric value `actionProbability` defines the marginal probability of `ActionProposal`.



**Fig. 3.** Action proposals in the MLN ontology TBox

## 5 Evaluation

The model presented above has been implemented and tested using the LTE simulator. This section presents evaluation of our system by analyzing sizes of the MLN and OWL model and then showing a visualization of the reasoning outcome.

### 5.1 Dataset Statistics

Table 3 clarifies the average sizes of the two models. As it can be seen, the rule base is the major part of both the MLN model (5450 rules) and the OWL 2 ontology (58000 triples). The high amount of MLN rules is due to the combinatorial generation of rules. The rule base could be optimized by removing insignificant rules, i.e. rules which have little or no impact on the inference in view of data used in analysis.

MLN evidence contains 100 lines which are processed into 1600 triples and 15 action proposals are processed into 70 triples. Altogether, the OWL 2 model is approximately 5.7 times bigger than the corresponding MLN model.

	Evidence	Rules	Action proposals	File size in MB
MLN model (lines)	100	5450	15	0.49
OWL 2 model (triples)	1600	58000	70	2.8

**Table 3.** Statistics of datasets

### 5.2 Visualization of the Reasoning Outcome

We have built an HTML5 application [1] to provide an empiric evaluation of the MLN reasoning results (action proposals). The interface is built by using faceted browsing activities and interactive visualization methods in order to support user's information exploration from RDF-based data. In figure 4 can be seen latest cell-specific action proposals and their relations to the evidence of the reasoner (latest KPI values). With respect to the facet selections user can examine the patterns that might occur between the network context and MLN reasoning. For example, the figure demonstrates that if a cell has high RLF value and low CQI value, it usually implies a proposal to increase the TXP of that cell.

## 6 Related Work

Reasoning under uncertainty has in the past been performed with a variety of methods, including Markov Networks [11], Bayesian Networks [14], as well as probabilistic extensions to description logic ontologies such as to OWL [7]. A more recent additional approach is the MLN [20], which makes it possible to compactly define statistical relational models containing both certain and uncertain facts as well as potentially contradictory pieces of data using First Order Logic (FOL). In the telecommunications field,

Facet settings		Cell Status					
Filter by Amount of neighbors:		ID	Rlf	Cqi	Neighbors	Txp-action	Ret-action
No selection		2			4	(0.81)	
Filter by Cqi:		3			4	(0.87)	
LowCqi		7			3	(0.86)	
Filter by Rlf:		12			4	(0.65)	
HighRlf							

**Fig. 4.** Visualization for MLN reasoning outcome and evidence

there have been plenty of research projects which adapt these techniques into different network management tasks. For example, Bayesian networks (BN) are proposed for automatic network fault management [9][2] and MLN to diagnose anomalous cells [4].

In mobile network research, ontologies have been used to model general concepts of the telecommunication field [17] as well as to model context in mobile network management [21][24]. The Linked Open Data (LOD)<sup>3</sup> paradigm has also been addressed in [22], where cells and terminals are modeled and combined with other data sources, for example, with event data. However, there exists no research of using ontologies and statistical reasoning together to analyze and configure the mobile network, as in this paper.

In other problem domains there have been experiments of combining an ontological approach with statistical relational learning. For example, Bayesian Networks and its relational extensions, such as multi-entity Bayesian networks (MEBN), have been applied with OWL ontologies in order to infer probabilistic results from a certain domain [6]. BN-specific projects have use cases, for example, for medical decision support [25], financial fraud detection [3], and instance matching in a geological domain [15].

MLNs have been applied with semantic technologies mainly in problem domains for ontology matching [13] and for natural language processing, in which ontological concepts are extracted from text [8][16]. Another model used for similar problems as MLN is the Infinite Hidden Relational Model (IHRM) [23] and its semantic extension, the Infinite Hidden Semantic Model (IHSM), which also combines certain and uncertain facts. This technique has been demonstrated in social network analysis. [19]

## 7 Conclusion and Future Work

We have generated a mapping from our MLN model into a consistent *SHIF* OWL 2 DL ontology. The OWL 2 model is currently utilized only as an RDF graph by using SPARQL queries (faceted navigation) in the HTML5 GUI. Advanced DL reasoning tasks has not yet been implemented.

The next step in this project is to enhance the OWL-MLN interaction so that MLN model settings can be dynamically modified by a human or a DL reasoner (Pellet). Model settings include selection of measurement variables, their threshold values and rules to be generated from the set of variables. Model settings could even include some

<sup>3</sup> <http://linkeddata.org/>

initial rule weights with respect to prior knowledge. Moreover, our system will be enhanced by creating high-level goals which the user can use to modify the behaviour of the reasoning system. For example, high-level goals could be mapped to corresponding MLN model settings.

Altogether, the practical reason to combine semantic technologies with statistical relational reasoning was to generalize the representation of the MLN model in order to make it semantically adaptable. Current implementation gives promising results to continue this work in order to enhance the system towards autonomic computing and towards managing a more dynamic and heterogeneous environment.

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